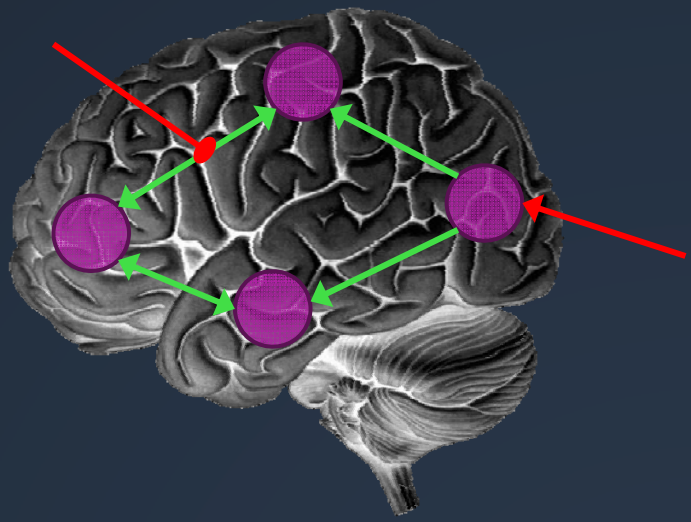
Effective Connectivity & the basics of Dynamic Causal Modelling



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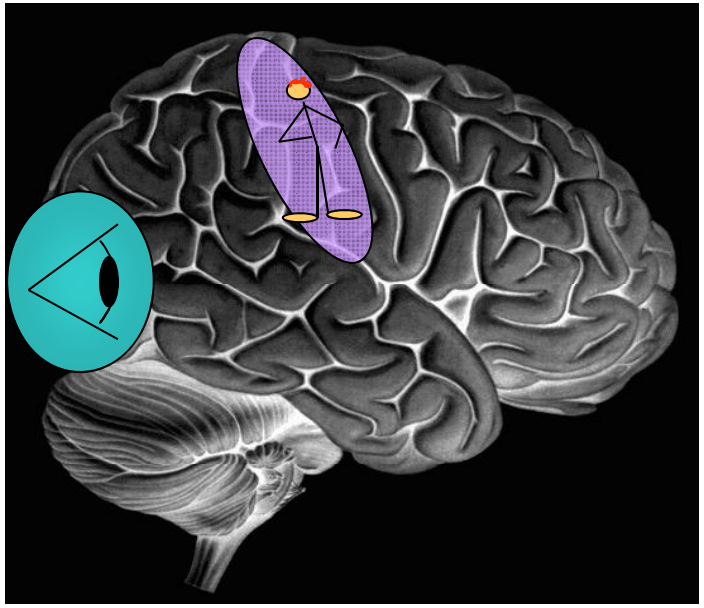
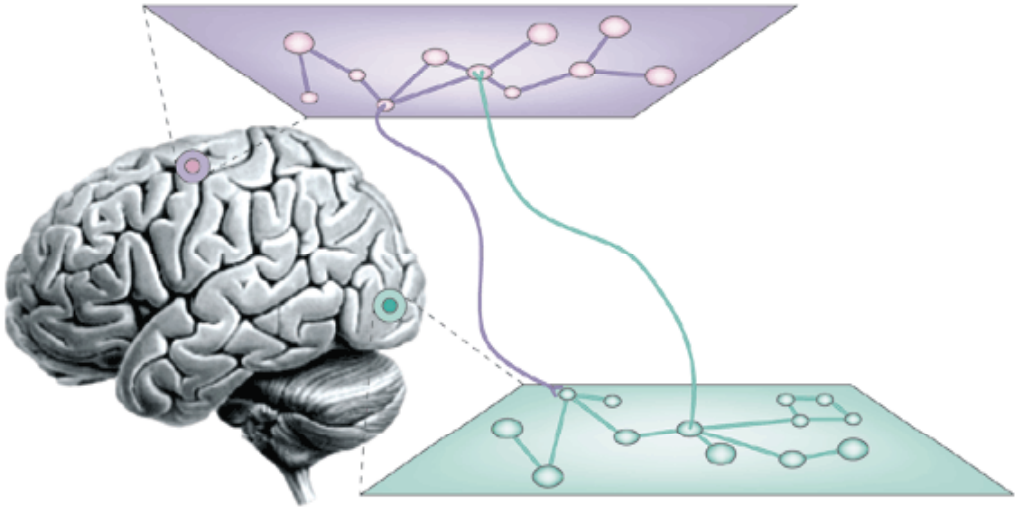
SPM course Zurich, February 15-17

Principles of organisation

Functional Specialisation



Functional Integration



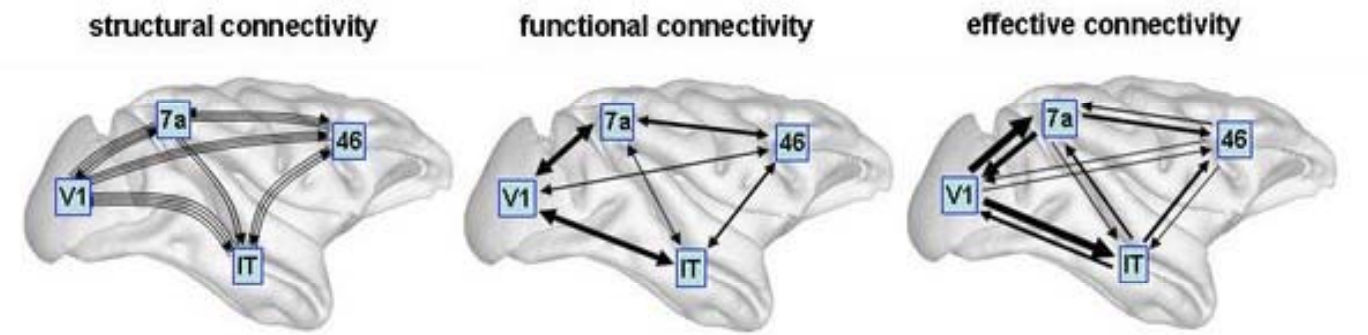
Overview

Brain Connectivity: types & definitions

Dynamic Causal Modelling – in theory

Dynamic Causal Modelling – in practice

Structural, functional & effective connectivity



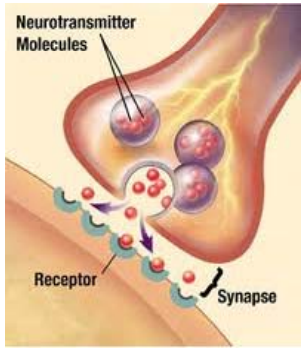
Sporns 2007, *Scholarpedia*

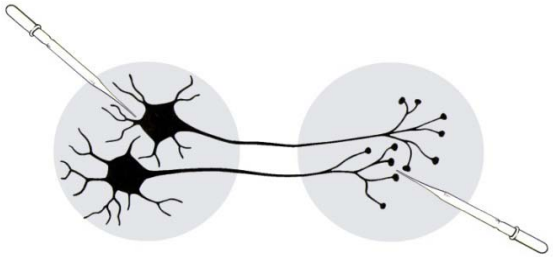
- **anatomical/structural connectivity**
  presence of axonal connections
- **functional connectivity**
  statistical dependencies between regional time series
- **effective connectivity**
  causal (directed) influences between neurons or neuronal populations

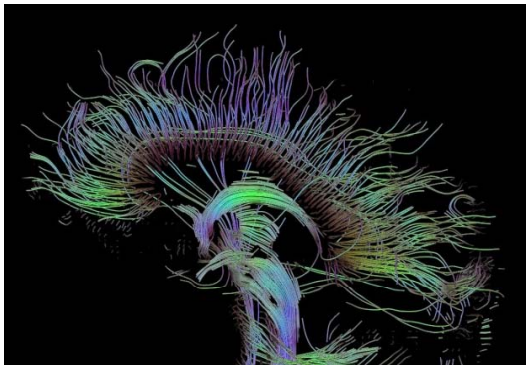
Anatomical connectivity

Presence of axonal connections

- neuronal communication via synaptic contacts
- Measured with
  - tracing techniques
  - diffusion tensor imaging (DTI)

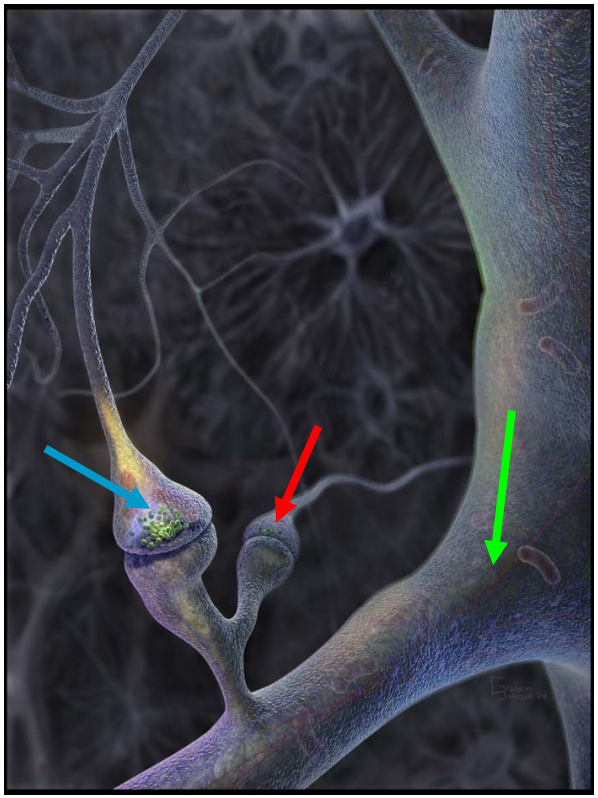






Knowing anatomical connectivity is not enough...

- Context-dependent recruiting of connections :
  - Local functions depend on network activity
- Connections show synaptic plasticity
  - change in the structure and transmission properties of a synapse
  - even at short timescales



Look at functional and effective connectivity

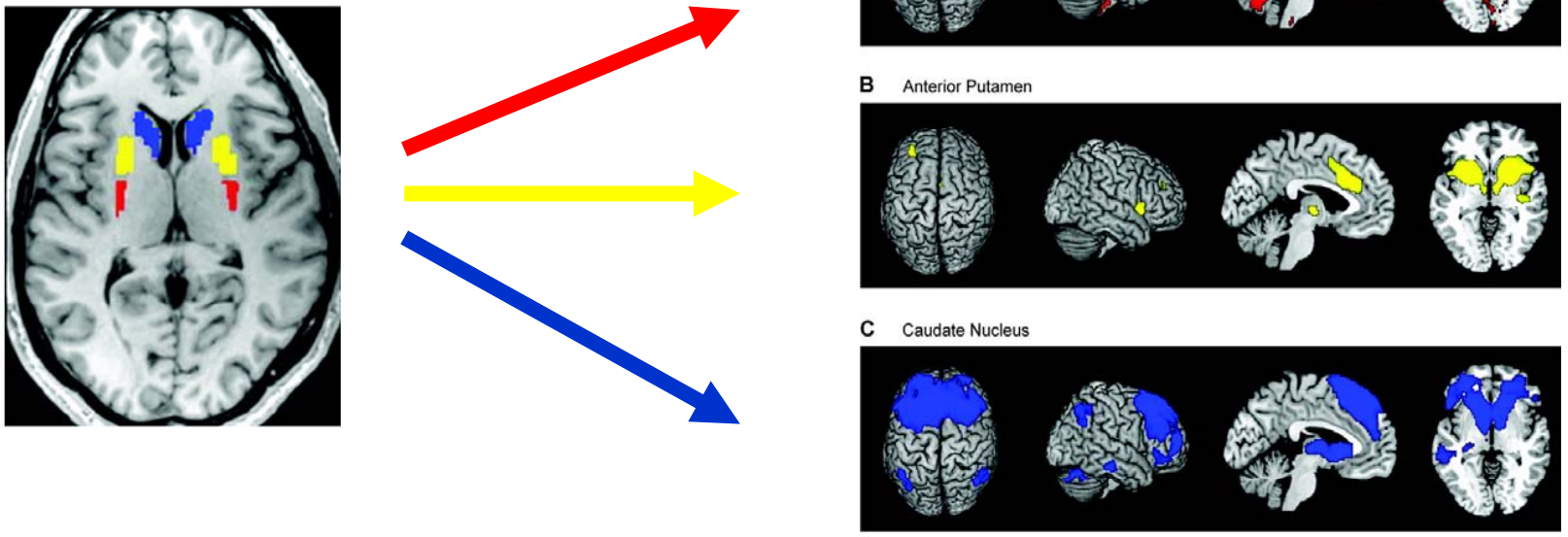
Functional Connectivity

Statistical dependencies between regional time series

- Seed voxel correlation analysis
- Coherence analysis
- Eigen-decomposition (PCA, SVD)
- Independent component analysis (ICA)
- any technique describing statistical dependencies amongst regional time series

Seed voxel correlation analyses

- hypothesis-driven choice of a seed voxel
- extract reference time series
- voxel-wise correlation with time series from all other voxels

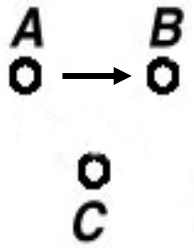


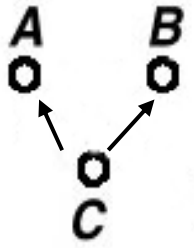
Functional Connectivity

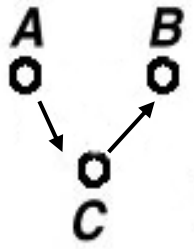
- Pro
  - useful when we have no experimental control over the system of interest and no model of what caused the data (e.g. sleep, hallucinations, etc.)

- Con
  - interpretation of resulting patterns is difficult / arbitrary
  - no mechanistic insight
  - usually suboptimal for situations where we have a priori knowledge / experimental control

Effective Connectivity



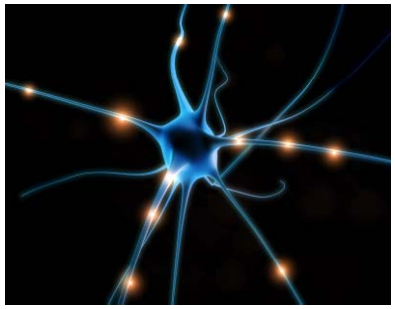




Effective Connectivity

Causal (directed) influences between neurons /neuronal populations

- *In vivo* and *in vitro* stimulation and recording
  -
  -
  -
  -
  -



- Models of causal interactions among neuronal populations
  - explain *regional* effects in terms of *interregional* connectivity

Models for computing effective connectivity in fMRI data

- Structural Equation Modelling (SEM)
  McIntosh et al. 1991, 1994; Büchel & Friston 1997; Bullmore et al. 2000
- Regression models
  (e.g. psycho-physiological interactions, PPIs)
  Friston et al. 1997
- Volterra kernels
  Friston & Büchel 2000
- Time series models (e.g. MAR, Granger causality)
  Harrison et al. 2003, Goebel et al. 2003
- Dynamic Causal Modelling (DCM)
  bilinear: Friston et al. 2003; *nonlinear:* Stephan et al. 2008

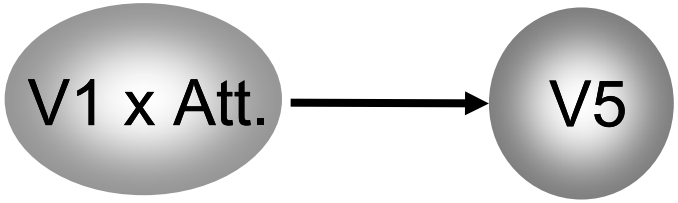
Psycho-physiological interactions (PPI)

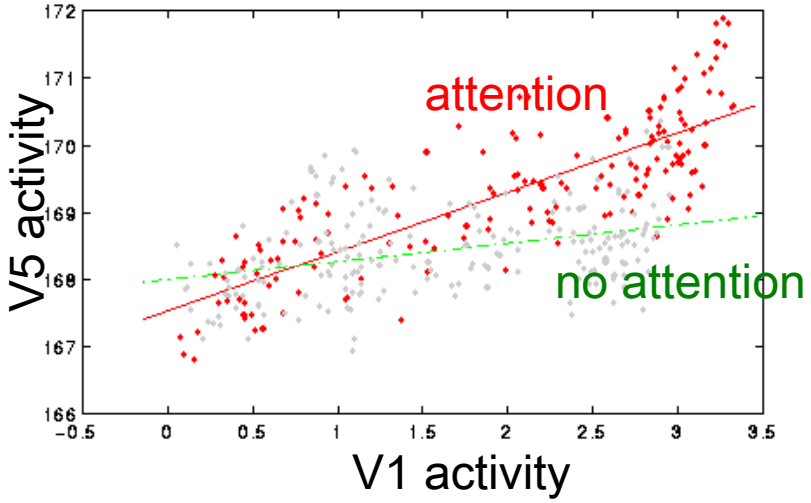
- Bilinear model of how the psychological context A changes the influence of area B on area C :

$$B \times A \rightarrow C$$

- Replace a (main) effect with the timeseries of a voxel showing that effect

- A PPI corresponds to differences in regression slopes for different contexts.





Psycho-physiological interactions (PPI)

- Pro
  - given a single source region, we can test for its context-dependent connectivity across the entire brain
  - easy to implement

- Con
  - only allows to model contributions from a single area
  - operates at the level of BOLD time series*
  - ignores time-series properties of the data *

* To be explained ☺

DCM for more robust statements of effective connectivity

Overview

Brain Connectivity: types & definitions

Dynamic Causal Modelling – in theory

- Basic idea
- Neural and hemodynamic levels
- Preview: priors & inference

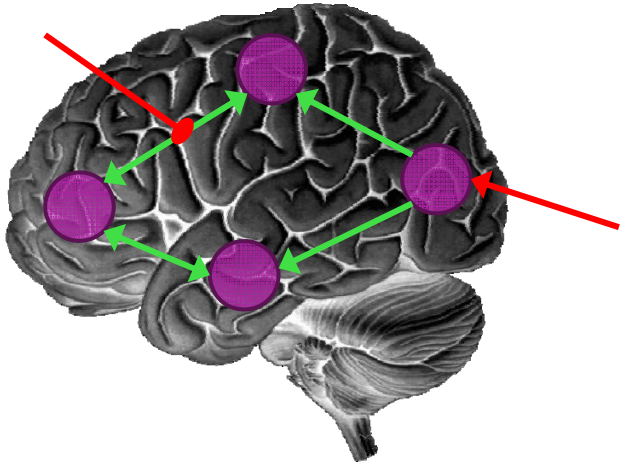
Dynamic Causal Modelling – in practice

DCM: the basics

DCM allows us to look at how areas within a network interact:

Investigate functional integration & modulation of specific cortical pathways

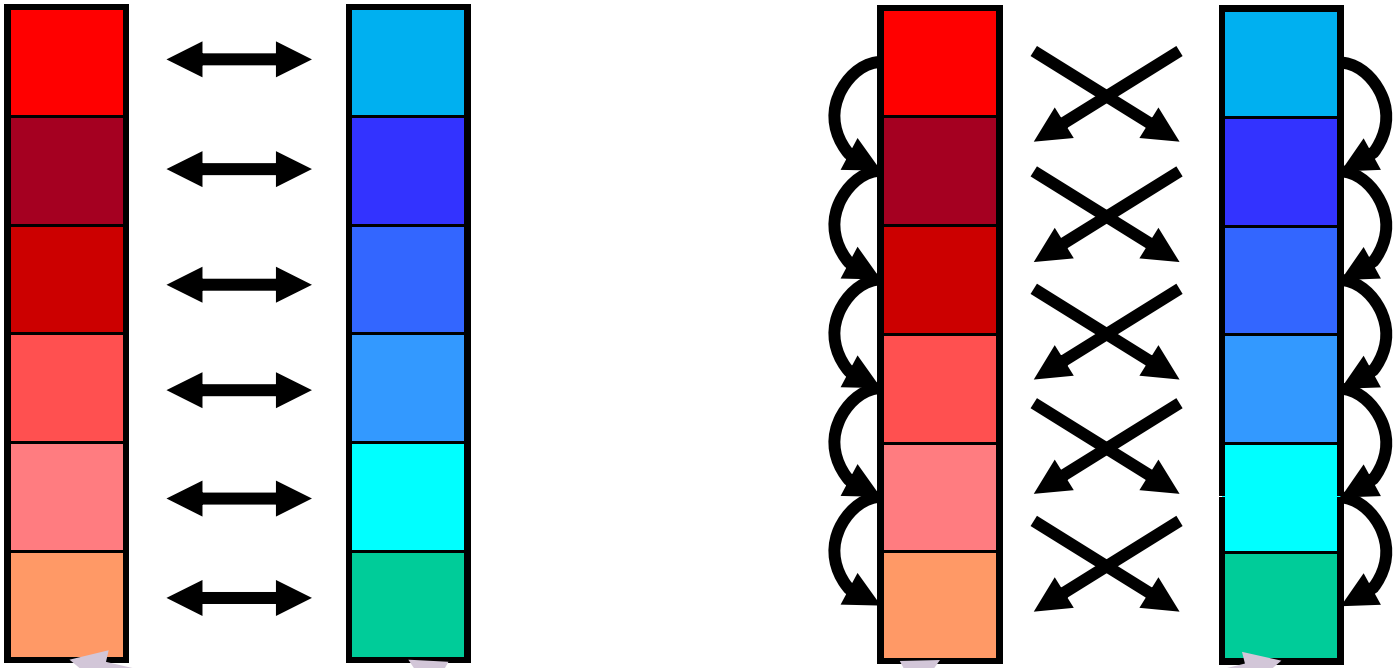
- Temporal dependency of activity within and between areas (causality)



Temporal dependence and causal relations

Seed voxel approach, PPI etc.

Dynamic *Causal* Models



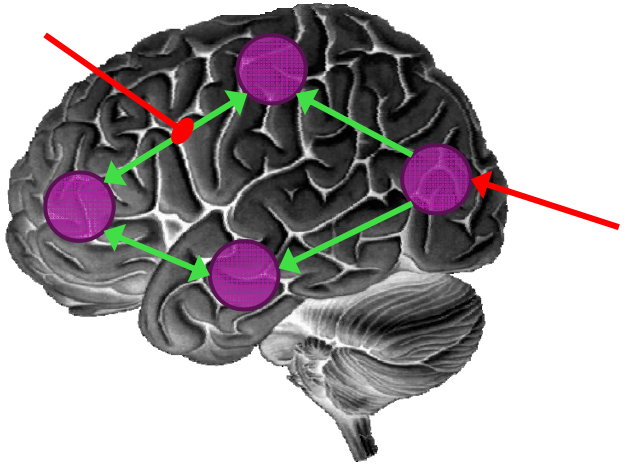
timeseries (neuronal activity)

DCM: the basics

DCM allows us to look at how areas within a network interact:

Investigate functional integration & modulation of specific cortical pathways

- Temporal dependency of activity within and between areas (causality)
- Separate neuronal activity from observed BOLD responses



DCM: Neuronal and hemodynamic level

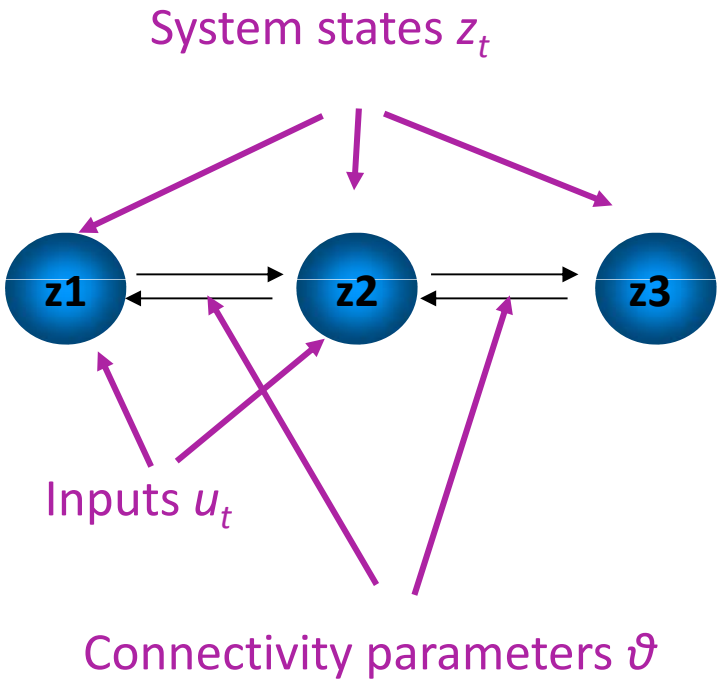
- Cognitive system is modelled at its underlying neuronal level (not directly accessible for fMRI).

- The modelled neuronal dynamics (**z**) are transformed into area-specific BOLD signals (**y**) by a hemodynamic model (λ).

The aim of DCM is to estimate parameters at the neuronal level such that the modelled and measured BOLD signals are maximally* similar

Neuronal model

- Aim: model temporal evolution of a set of neuronal states z_t



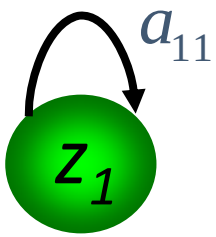
State changes are dependent on:

- the current state z
- external inputs u
- its connectivity ϑ

$$\frac{dz}{dt} = F(z, u, \theta)$$

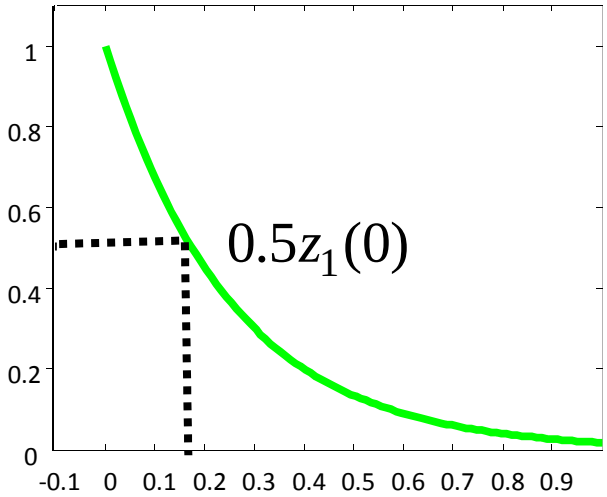
Why are DCM parameters rate constants?

Integration of a 1st order linear differential equation gives an exponential function:



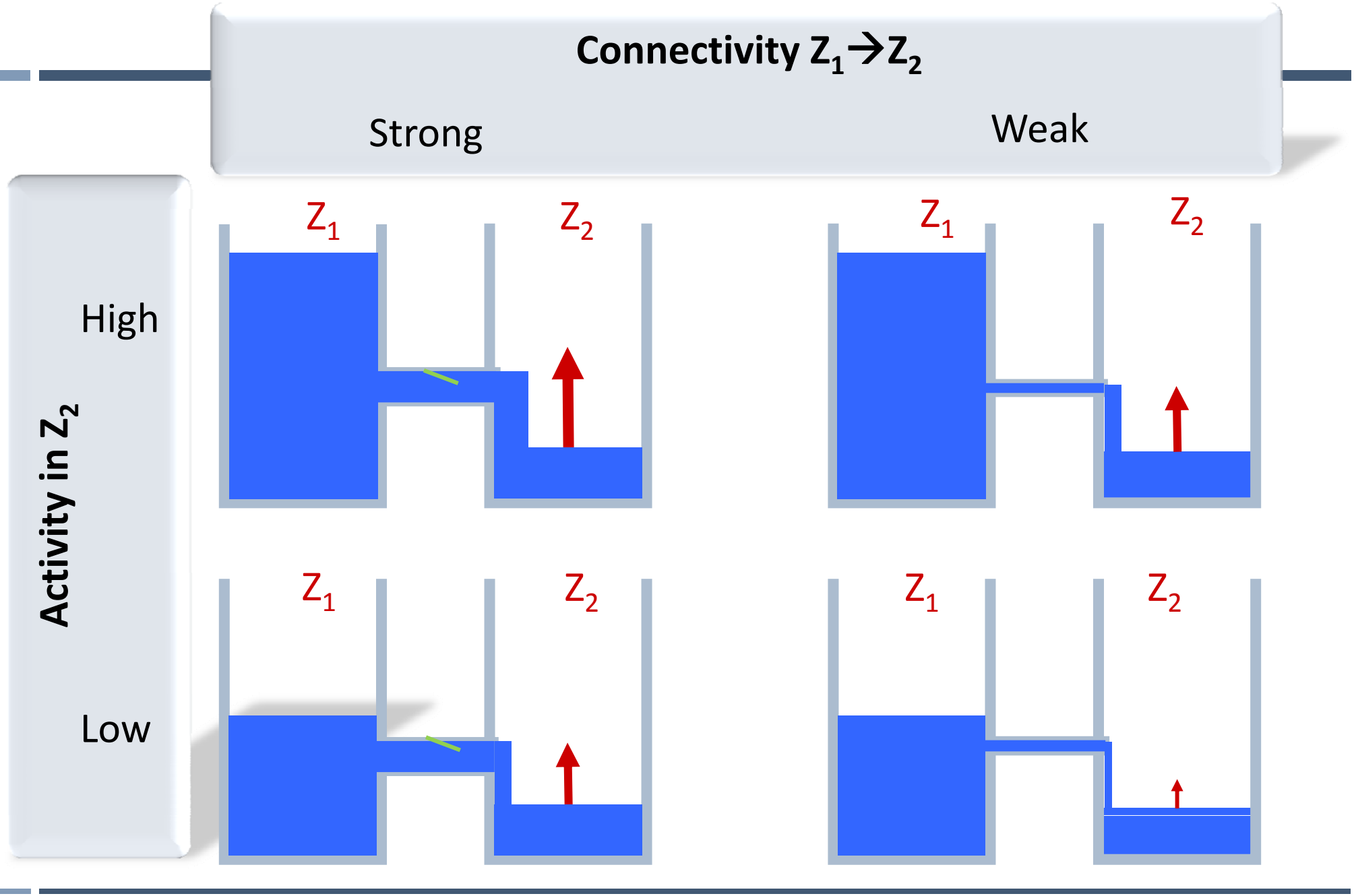
$$\frac{dz_1}{dt} = a_{11} z_1 \quad \rightarrow \quad z_1(t) = z_1(0)\exp(a_{11}t)$$

Decay function

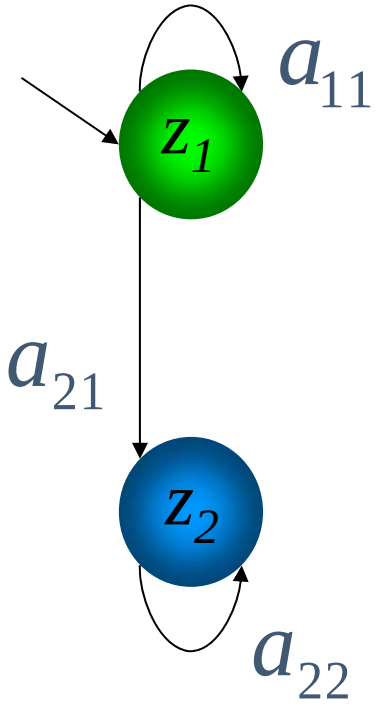


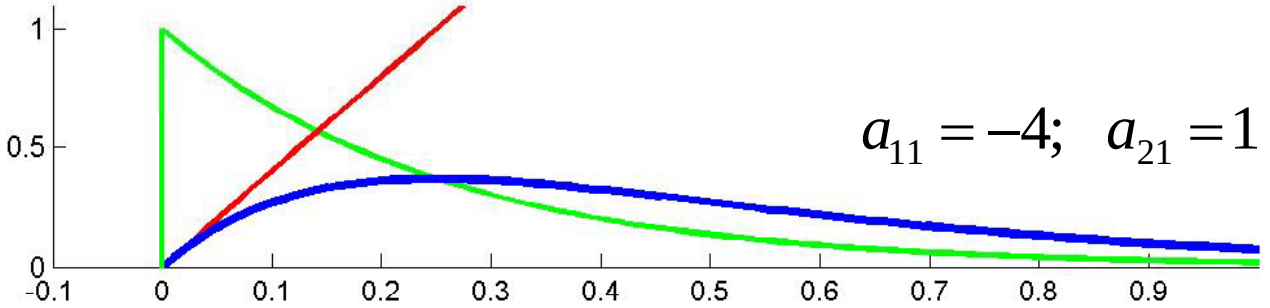
$$\tau = \ln 2 / s$$

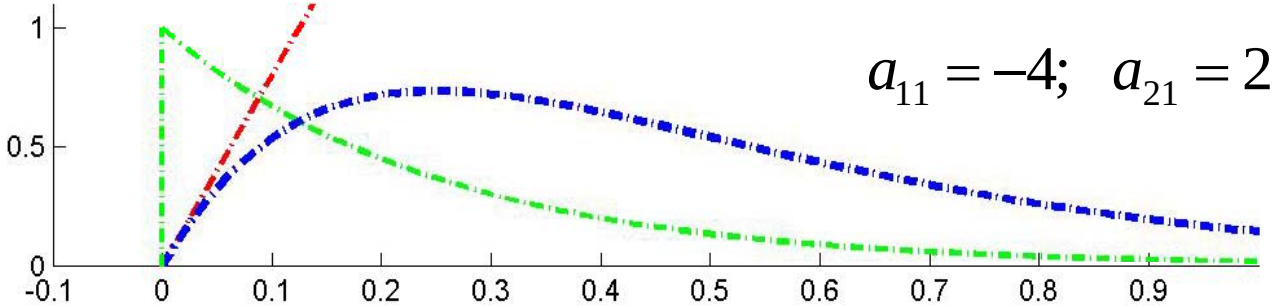
If $z_1 \rightarrow z_1$ is -0.10 s^{-1} this means that, per unit time, the decrease in activity in z_1 corresponds to 10% of the current activity in z_1

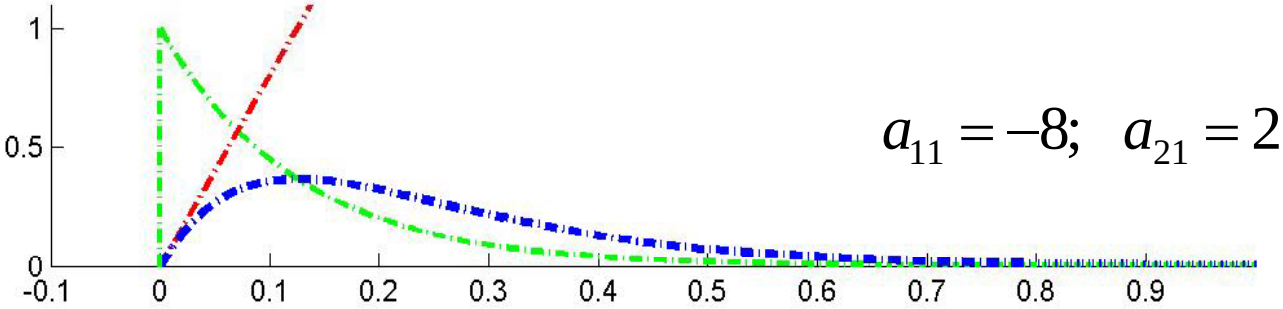

Connectivity $Z_1 \rightarrow Z_2$
Strong
Weak
Activity in Z_2
High
Low
Z_1
Z_2
Z_1
Z_2
Z_1
Z_2
Z_1
Z_2

Neurodynamics: 2 nodes with input

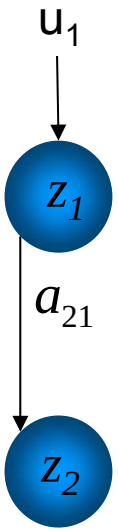




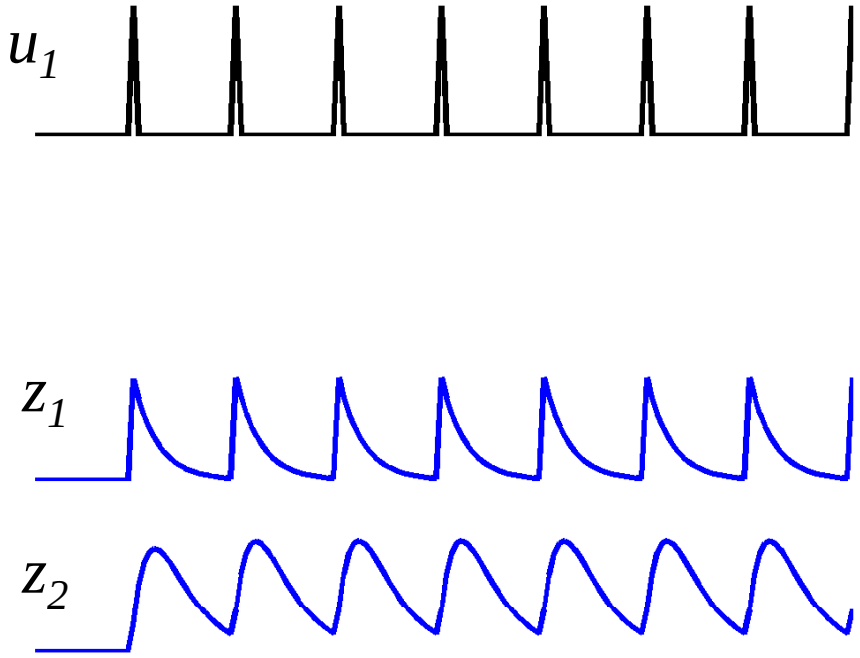




Neurodynamics: 2 nodes with input



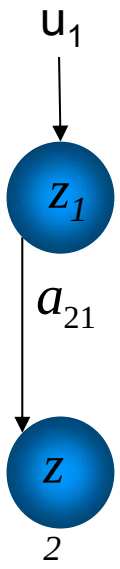
activity in z_2 is coupled to z_1 via coefficient a_{21}



$$\dot{z}_1 = a_{11} z_1 + c_{11} u_1$$
$$\dot{z}_2 = a_{21} z_1 + a_{22} z_2$$

$$\begin{bmatrix} \dot{z}_1 \\ \dot{z}_2 \end{bmatrix} = \begin{bmatrix} a_{11} & 0 \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} + \begin{bmatrix} c_{11} \\ 0 \end{bmatrix} u_1$$

Neurodynamics: 2 nodes with input



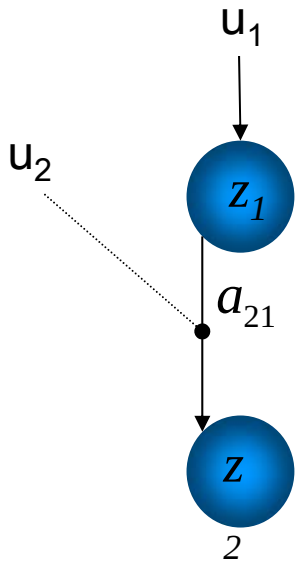
activity in z_2 is coupled to z_1 via coefficient a_{21}

$$\dot{z} = Az + Cu$$
$$\theta = \{A, C\}$$

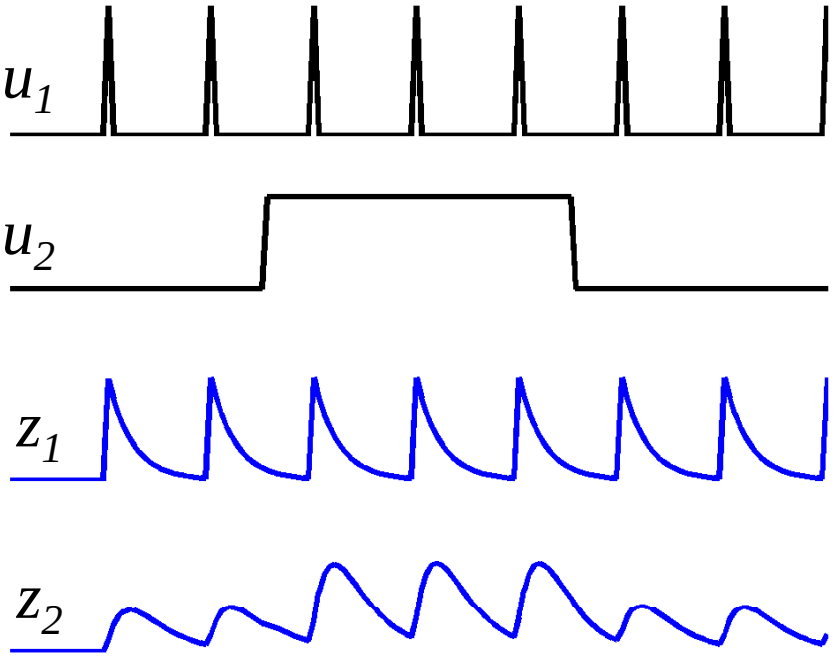
$$\dot{z}_1 = a_{11} z_1 + c_{11} u_1$$
$$\dot{z}_2 = a_{21} z_1 + a_{22} z_2$$

$$\begin{bmatrix} \dot{z}_1 \\ \dot{z}_2 \end{bmatrix} = \begin{bmatrix} a_{11} & 0 \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} + \begin{bmatrix} c_{11} \\ 0 \end{bmatrix} u_1$$

Neurodynamics: modulatory input



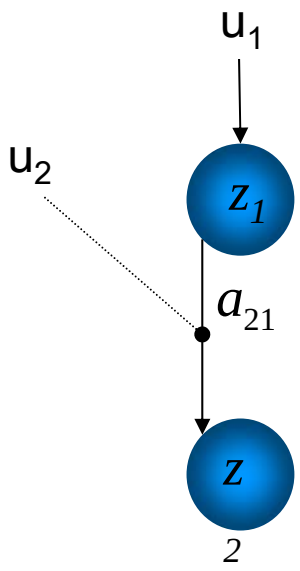
Modulatory input u_2 activity through coefficient a_{21}



$$\dot{z}_1 = a_{11} z_1 + c_{11} u_1$$

$$\dot{z}_2 = (a_{21} + b_{21}^2 u_2) z_1 + a_{22} z_2$$

Neurodynamics: modulatory input



Modulatory input
u_2 activity
through
coefficient a_{21}

$$\begin{bmatrix} \dot{z}_1 \\ \dot{z}_2 \end{bmatrix} = \begin{bmatrix} a_{11} & 0 \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} + u_2 \begin{bmatrix} 0 & 0 \\ b_{21}^2 & 0 \end{bmatrix} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} + \begin{bmatrix} c_{11} & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$$

$$\dot{z}_1 = a_{11} z_1 + c_{11} u_1$$

$$\dot{z}_2 = (a_{21} + b_{21}^2 u_2) z_1 + a_{22} z_2$$

Neurodynamics: bilinear neural state equation

$$\dot{z} = \left(A + \sum_{j=1}^{m} u_j B^{(j)} \right) z + Cu$$

$$\theta = \{A, B, C\}$$

state changes

connectivity

modulation of connectivity

state vector

direct inputs

external inputs

$$\begin{bmatrix} \dot{z}_1 \\ \vdots \\ \dot{z}_n \end{bmatrix} = \left\{ \begin{bmatrix} a_{11} & \cdots & a_{1n} \\ \vdots & \ddots & \vdots \\ a_{n1} & \cdots & a_{nn} \end{bmatrix} + \sum_{j=1}^{m} u_j \begin{bmatrix} b_{11}^j & \cdots & b_{1n}^j \\ \vdots & \ddots & \vdots \\ b_{n1}^j & \cdots & b_{nn}^j \end{bmatrix} \right\} \begin{bmatrix} z_1 \\ \vdots \\ z_n \end{bmatrix} + \begin{bmatrix} c_{11} & \cdots & c_{1m} \\ \vdots & \ddots & \vdots \\ c_{n1} & \cdots & c_{nm} \end{bmatrix} \begin{bmatrix} u_1 \\ \vdots \\ u_m \end{bmatrix}$$

n regions

m mod inputs

m direct inputs

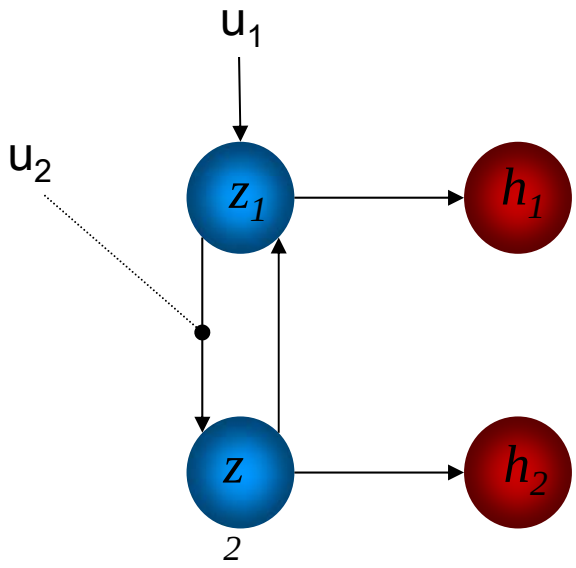
DCM: Neuronal and hemodynamic level

- Cognitive system is modelled at its underlying neuronal level (not directly accessible for fMRI).

- The modelled neuronal dynamics (**z**) are transformed into area-specific BOLD signals (**y**) by a hemodynamic model (λ).

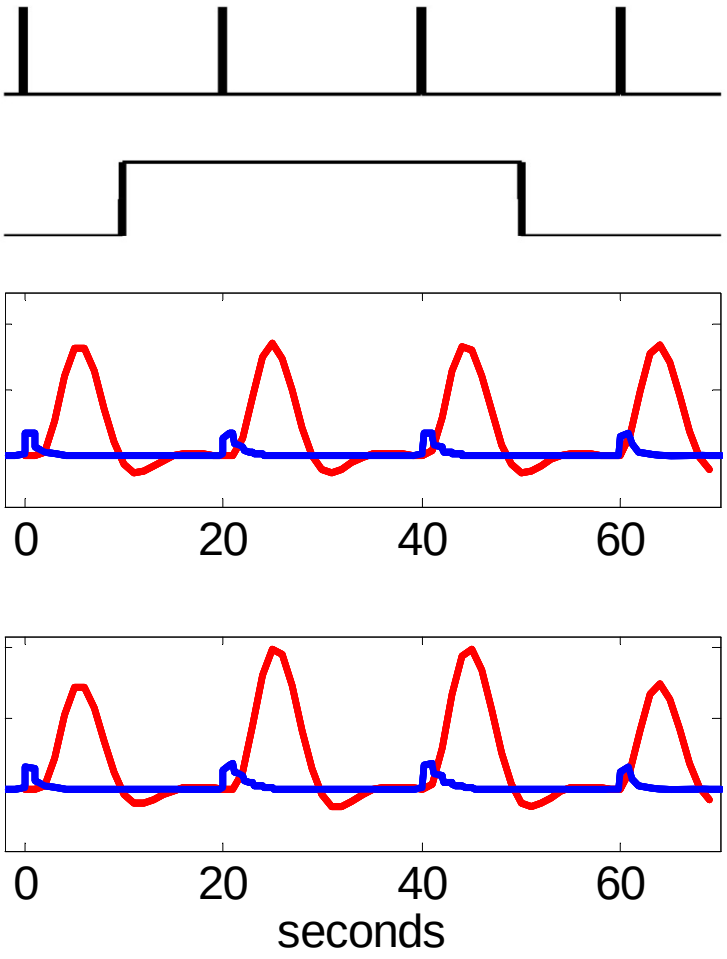
Hemodynamics: reciprocal connections

h(u,θ) represents the modelled BOLD response (balloon model) to the neural dynamics



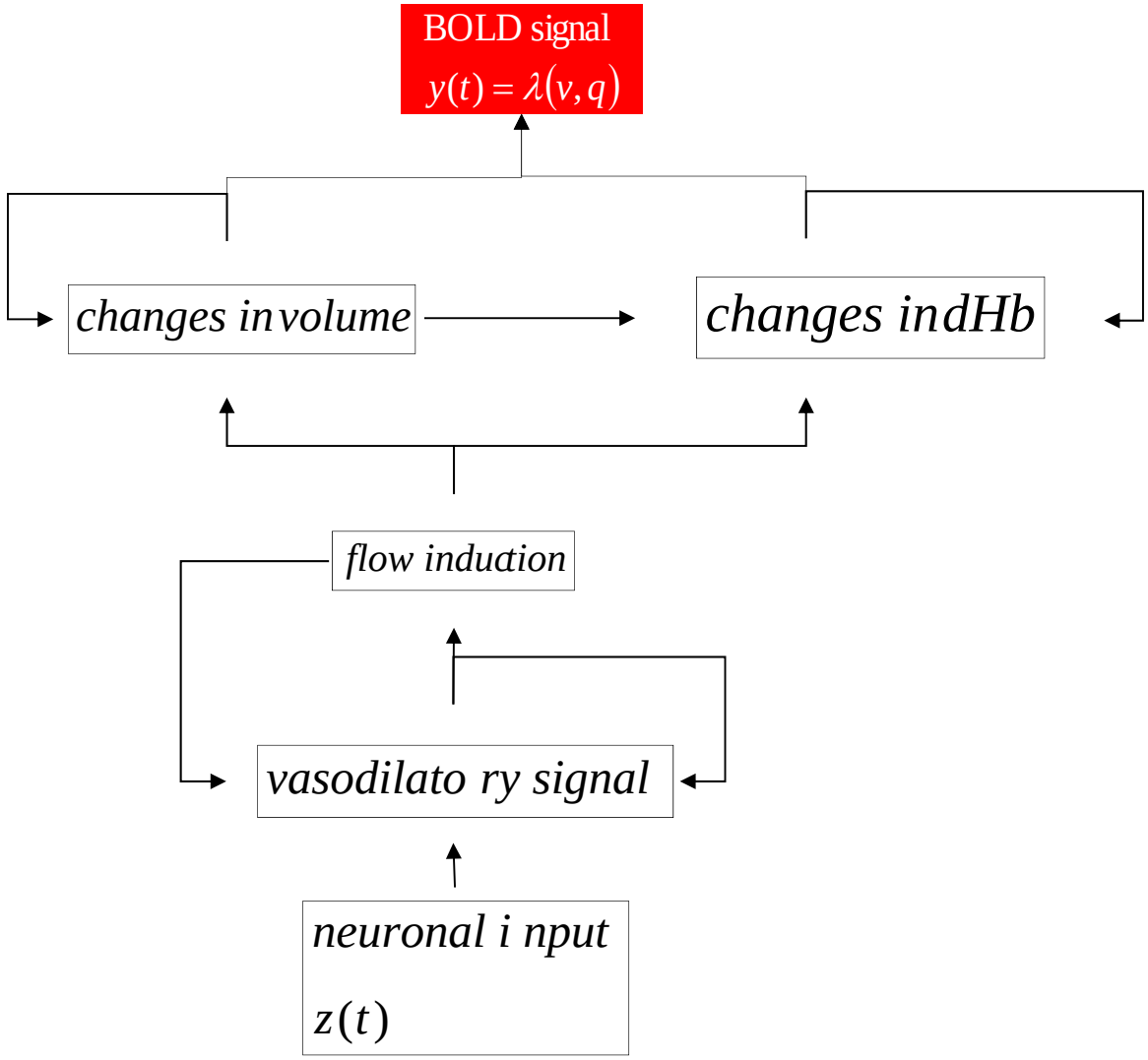
Z: neuronal activity

H: BOLD response



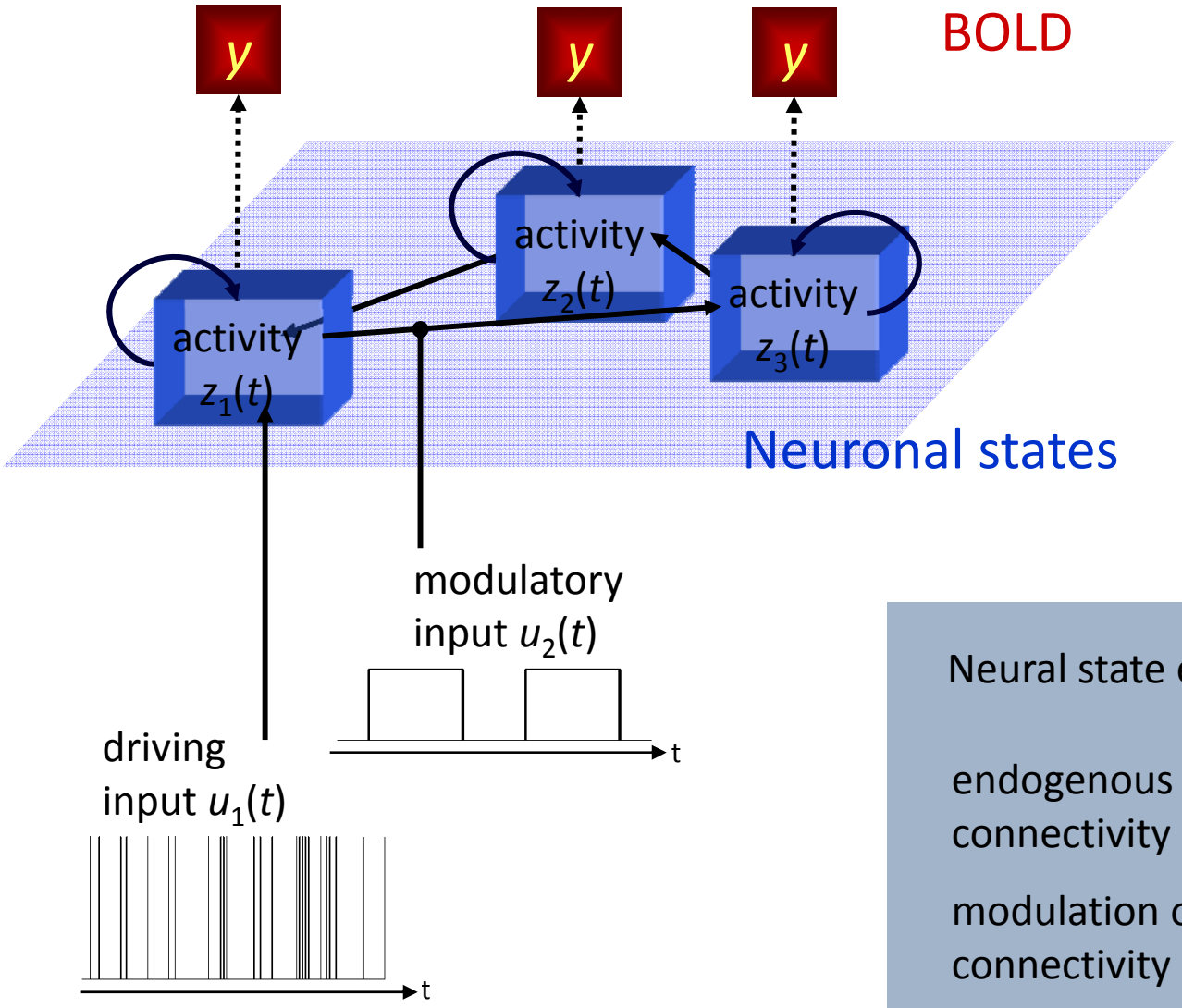
The hemodynamic "Balloon" model

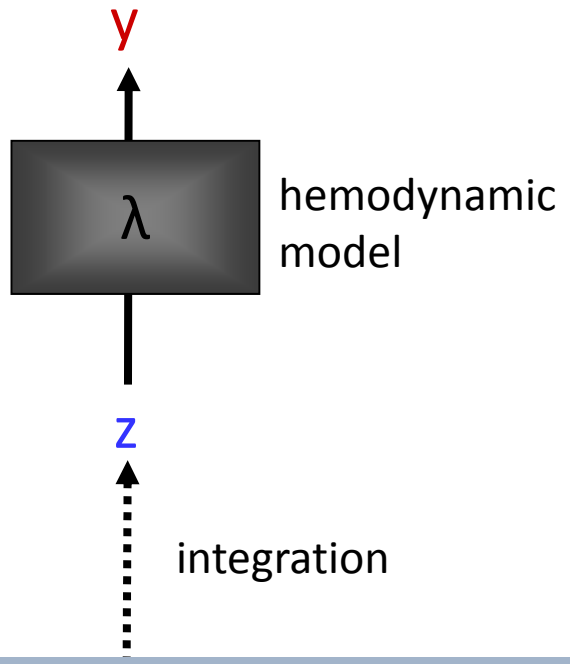
- 3 hemodynamic parameters
- Important for model fitting, but of no interest
- Computed separately for each area → region-specific HRFs



Friston et al. 2000, *NeuroImage*
Stephan et al. 2007, *NeuroImage*

DCM for fMRI: the full picture





Neural state equation $\dot{z} = (A + \sum u_j B^{(j)})z + Cu$

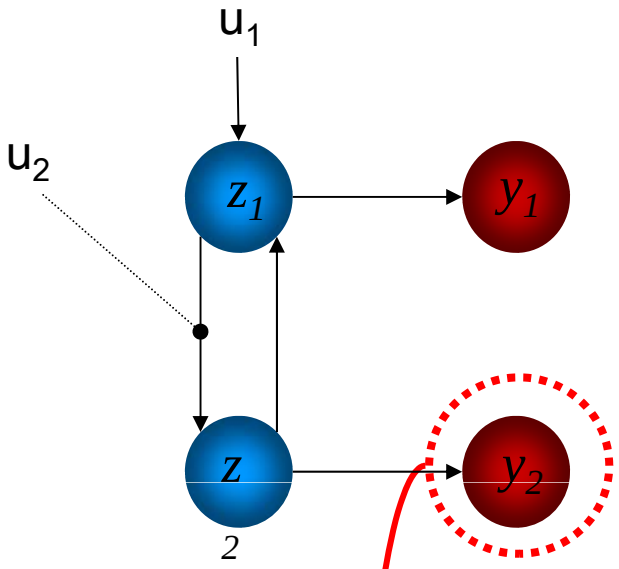
endogenous connectivity $A = \frac{\partial \dot{z}}{\partial z}$

modulation of connectivity $B^{(j)} = \frac{\partial}{\partial u_j}\frac{\partial \dot{z}}{\partial z}$

direct inputs $C = \frac{\partial \dot{z}}{\partial u}$

Stephan & Friston (2007), *Handbook of Brain Connectivity*

Modelled and measured BOLD signal

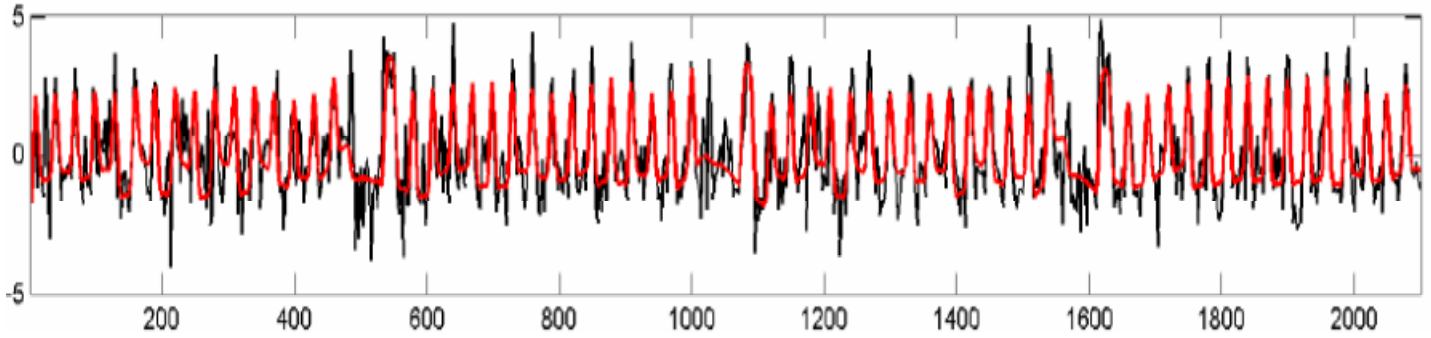


Recap

The aim of DCM is to estimate

- neural parameters {A, B, C}
- hemodynamic parameters

such that the **MODELLED** and **MEASURED** BOLD signals are maximally



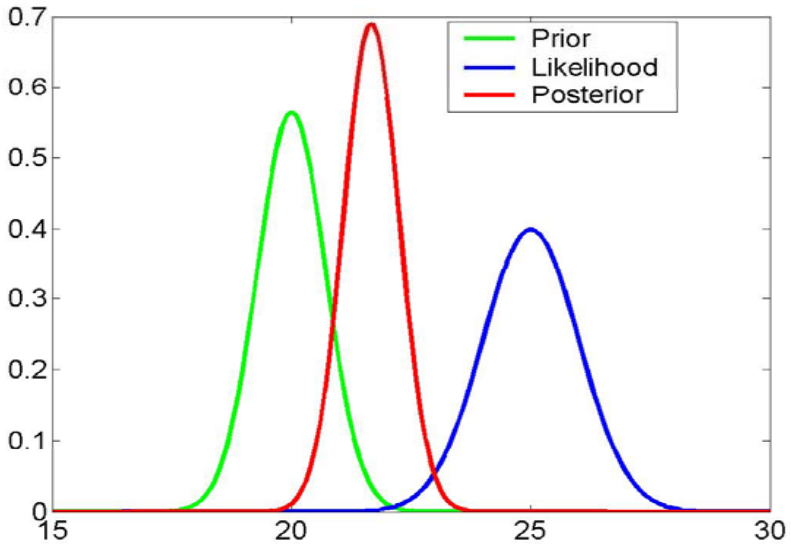
Bayesian statistics: Priors in DCM

Express our prior knowledge or "belief" about parameters of the model

posterior $\propto$ likelihood $\cdot$ prior

$$p(\theta \mid y) \propto p(y \mid \theta)p(\theta)$$

new data prior knowledge



Parameters governing

- Hemodynamics in a single region
- Neuronal interactions

Constraints (priors) on

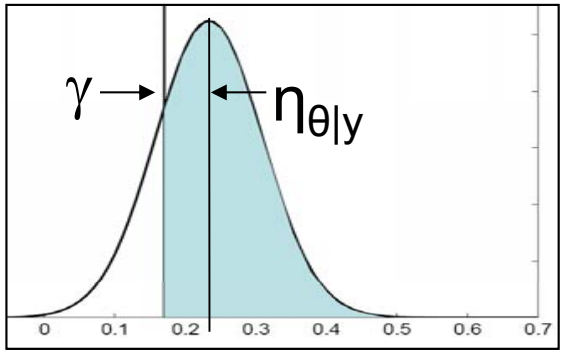
- Hemodynamic parameters
  - Empirical
- Self connections
  - principled
- Other connections
  - shrinkage

Inference about DCM parameters

Bayesian single subject analysis

The model parameters are distributions that have a mean $\eta_{\theta|y}$ and covariance $C_{\theta|y}$.

- Use of the cumulative normal distribution to test the probability that a certain parameter is above a chosen threshold γ:



Classical frequentist test across Ss

Test summary statistic: mean $\eta_{\theta|y}$

- One-sample t-test: Parameter > 0?
- Paired t-test:
  parameter 1 > parameter 2?

Bayesian model averaging

Overview

Brain Connectivity: types & definitions

Dynamic Causal Modelling – in theory

Dynamic Causal Modelling – in practice

- Design of experiments and models
- Simulated data
- Connectivity in synesthesia

Planning a DCM compatible study

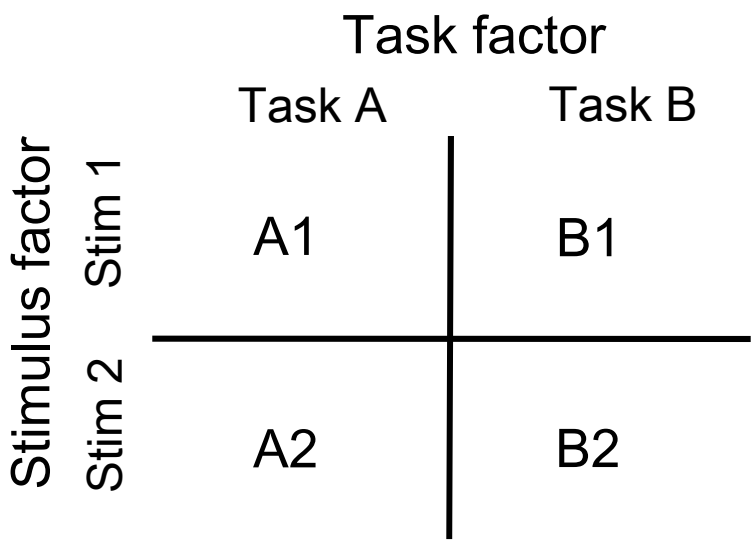
Suitable experimental design:

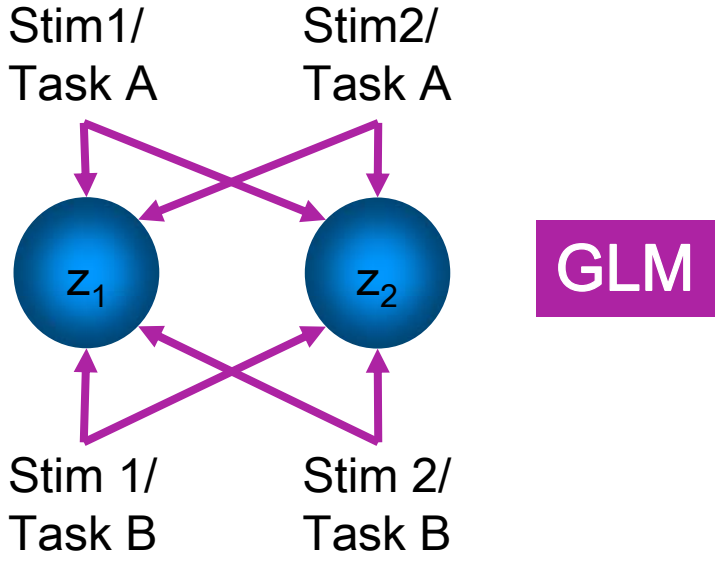
- any design that is suitable for a GLM
- preferably multi-factorial (e.g. 2 x 2)
  - e.g. one factor that varies the driving (sensory) input
  - and one factor that varies the contextual input

Hypothesis and model:

- Define specific *a priori* hypothesis
- Define model space: What are the alternative models?
- Define criteria for inference
  - Which parameters are relevant to test your hypothesis?
- If you want to verify that intended model is suitable to test this hypothesis, use simulations

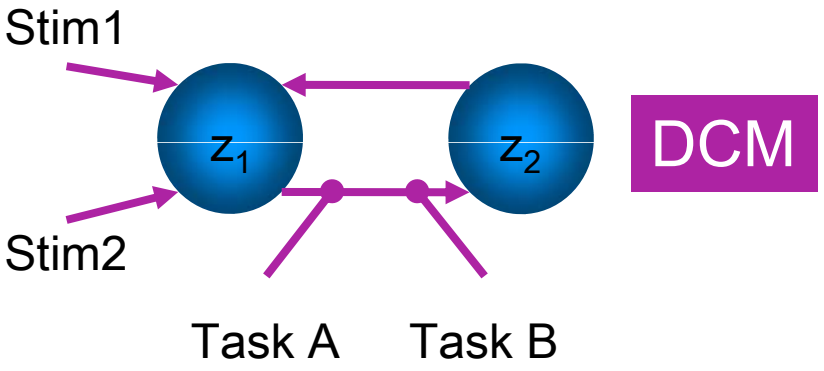
Multifactorial design: explaining interactions with DCM



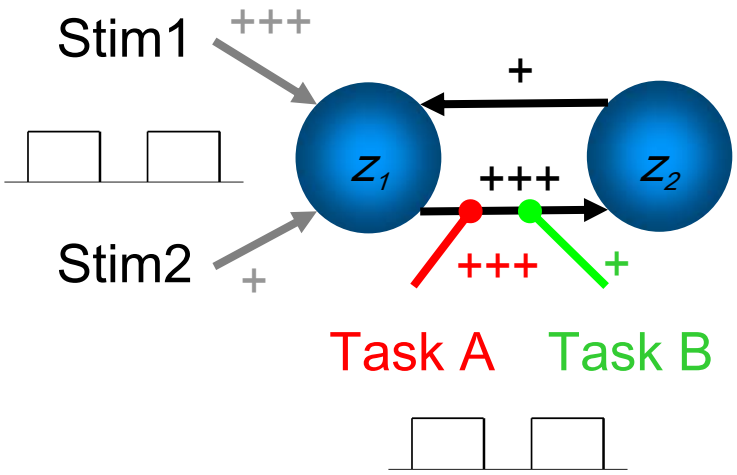


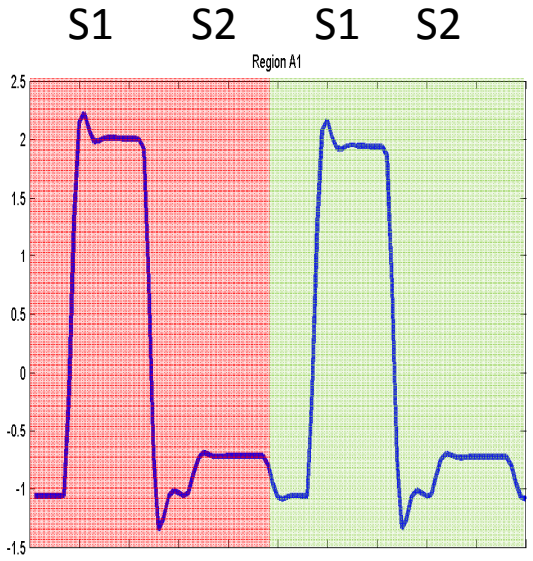
Let's assume that an SPM analysis shows a main effect of stimulus in z_1 and a stimulus × task interaction in z_2.

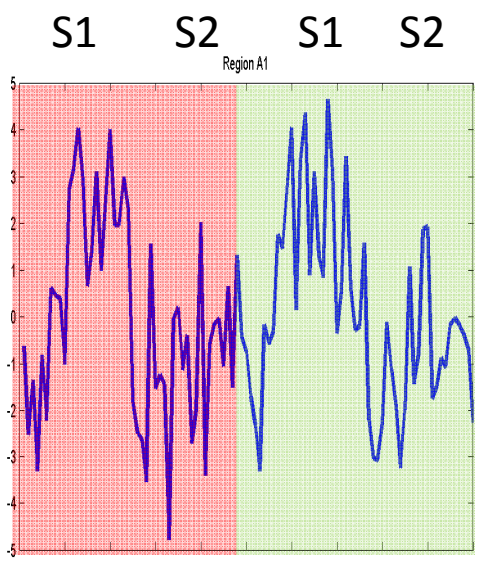
How do we model this using DCM?



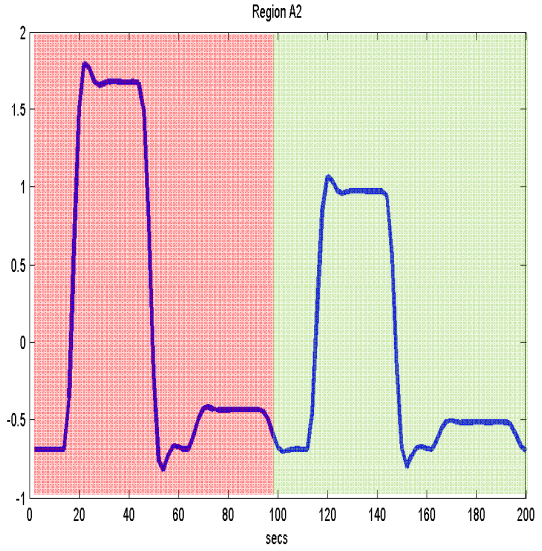
Simulation

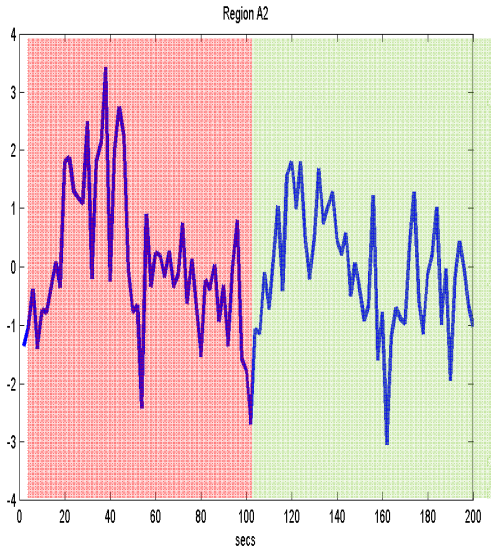






z_1

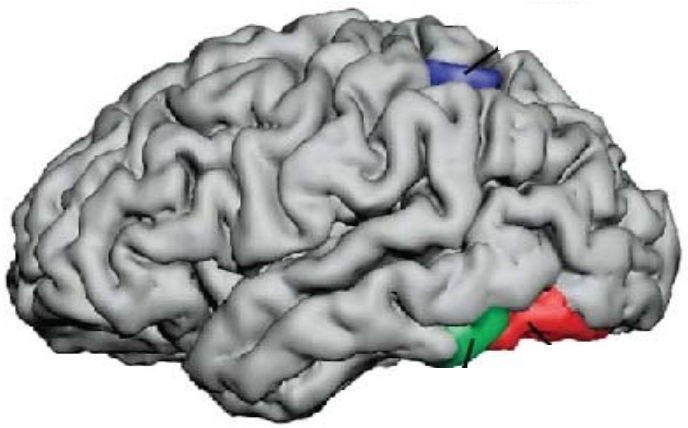




z_2

An Example: Brain Connectivity in Synesthesia

- Specific sensory stimuli lead to unusual, additional experiences
- Grapheme-color synesthesia: **color**
- Involuntary, automatic; stable over time, prevalence ~4%
- Potential cause: aberrant **cross-activation** between brain areas
  - grapheme encoding area
  - color area V4
  - superior parietal lobule (SPL)



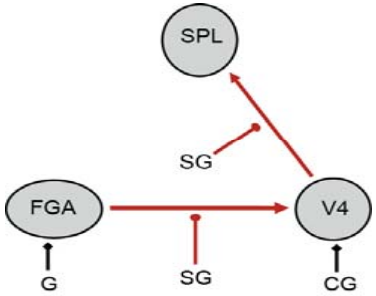
Hubbard, 2007

Can changes in effective connectivity explain synesthesia activity in V4?

An Example: Brain Connectivity in Synesthesia

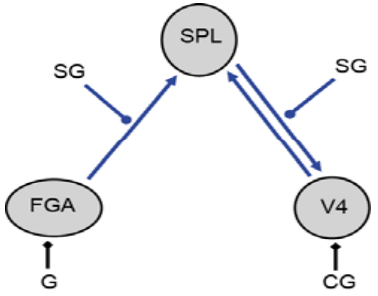
Bottom-up

(*Ramachandran & Hubbard, 2001*)



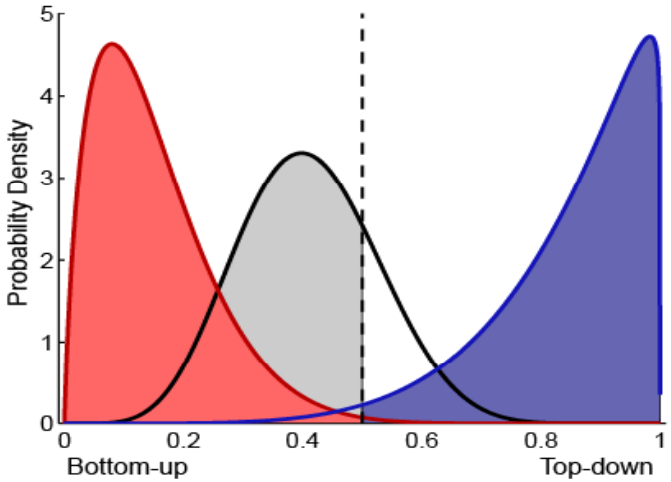
Top-down

(*Grossenbacher & Lovelace, 2001*)

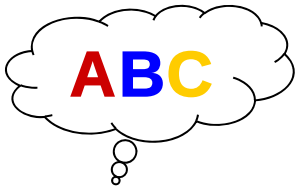


Projectors

ABC



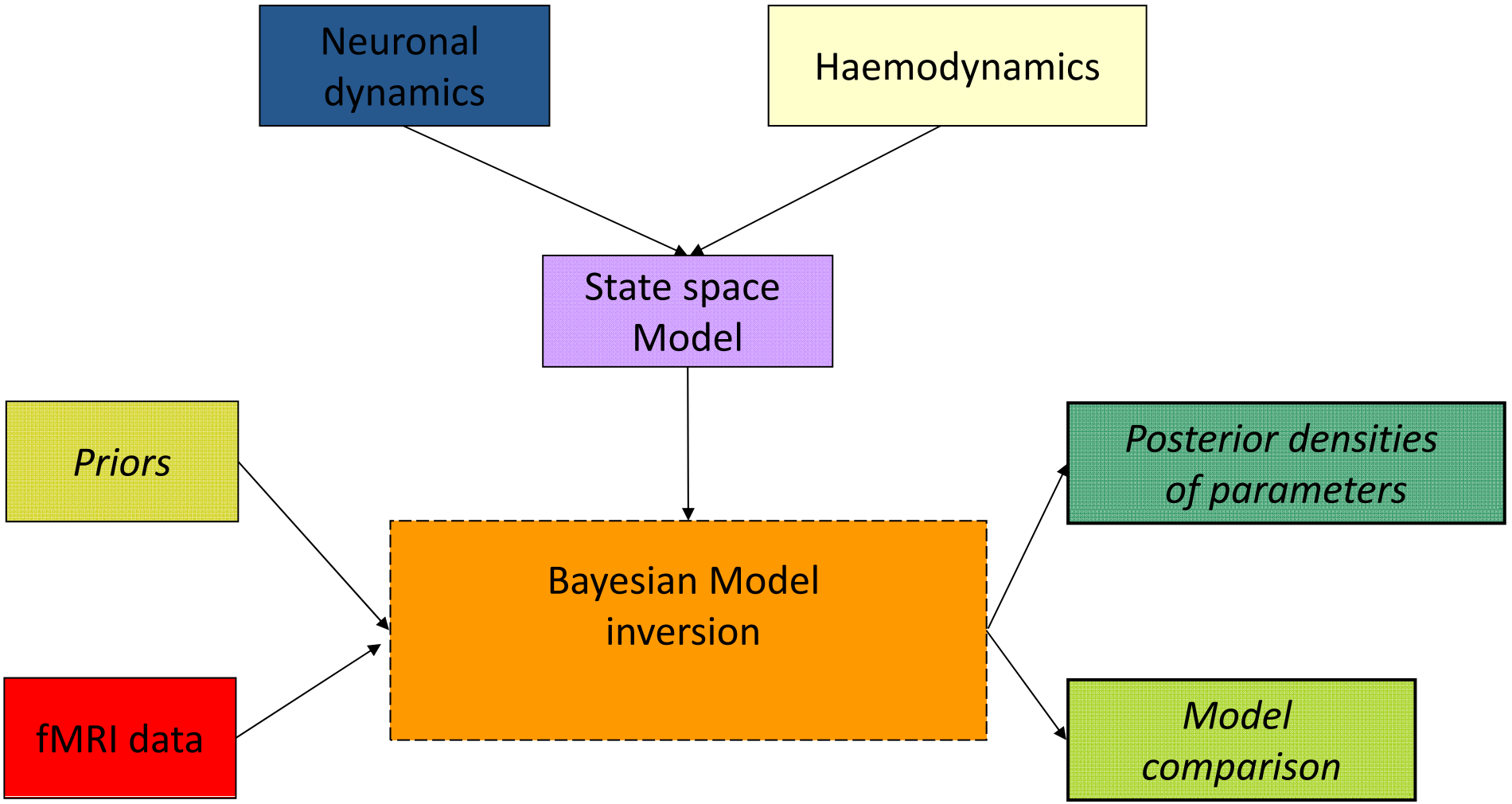
Associators



ABC

Effective connectivity determines conscious experiences…!

Summary: DCM Roadmap



Some useful references

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